# SAFE-FOLLOWING DISTANCES BASED ON THE CAR-FOLLOWING MODEL

Ponlathep Lertworawanich, Ph.D.

Bureau of Road Research and Development Department of Highways Sri-Ayudhaya Road, Ratchatevi Bangkok 10400 Thailand Email: ponla\_le@doh.go.th

#### ABSTRACT

Nowadays transportation forms an integral part of social activities. Unfortunately, one of the by-products of modern transportation is the price that society pays for injury and loss of life. In Thailand there are more than 100,000 traffic accidents and traffic-related casualties of approximately 12,000 deaths per year. Regardless of which formula one uses to compute the monetary loss and the physiological and psychological stress due to these accidents, the true cost to society is so great that it defies comprehension.

Even though there is no specific statistic in Thailand, it is thought that rear-end collision is the most common type of road accidents. Therefore, the aim of this research is to mitigate or reduce the severity and the number of road accidents, especially rear-end collisions by introducing a safe-following distance concept. This research developed a methodology to estimate the safe car-following distance for a speed range from 80 to 120 km/h within which speeds are commonly observed on the national highways of Thailand. The proposed is based on the maximum likelihood estimation and perturbation technique to derive the safe following distance. In order to bring the findings of this research into practice, the "dot" tailgating treatment marking is developed as a safety countermeasure for assisting drivers in establishing the recommended following distance.

## **1. INTRODUCTION**

A lot has happened in the world. The dramatic political events, complex changes in the global economy, and major advances in information and technology have been perceived. It is very likely that such developments will continue in the days and years ahead. Yet, even as we step toward the future, important ethical and social issues of human rights, consumer awareness, environmental protection, health, and education remain of pressing concern. Nowadays transportation forms an integral part of social activities. Unfortunately, one of the by-products of modern transportation is the price that society pays for injury and loss of life. No one who lives in a motorized society can fail to be concerned about the enormous human cost of traffic crashes. In Thailand there are more than 100,000 traffic accidents and traffic-related casualties of approximately 12,000 deaths per year. These numbers are very likely to escalate with the welcomed economic growth. Regardless of which formula one uses to compute the monetary loss and the physiological and psychological stress due to these accidents, the true cost to society is so great that it defies comprehension.

The Department of Highways (DOH) is responsible for planning, designing, constructing, and maintaining national highways throughout Thailand. It is therefore the urgent obligations of the DOH to provide both safe and efficient land transport to the public simultaneously. Even though there is no specific statistic in Thailand, it is thought that rearend collision is the most common type of road accidents. Many people have experienced the frustration of traveling behind slow-moving vehicles. Under these conditions, many drivers, especially aggressive drivers, are tempted to follow more closely than they should. This practice, commonly referred to as "tailgating," is risky and can lead to rear-end collisions or other accidents. When drivers tailgate, they significantly reduce their stopping distance or the distance needed to come to a complete and safe stop. Apparently, the more space drivers allow between their vehicles and the vehicles in front of them, the more time they have to see a hazard and react safely.

Car-following theory is one of the most widely used models to explain how vehicles follow one another in a traffic stream. The theory was first developed in the 1950s and continues to be developed today. In general, the relative simple and common driving task of one vehicle following another on a straight roadway where there is no passing can be categorized in three specific subtasks:

- Perception: the driver collects relevant information mainly through the visual channel. This information arises primarily from the motion of the lead vehicle and the driver's vehicle.
- Decision Making: a driver interprets the information obtained by sampling and integrates it over time in order to provide adequate updating of inputs.
- Control: The skilled driver can execute control commands with dexterity, smoothness, and coordination, constantly relying on feedback from his own responses which are superimposed on the dynamics of car-following system.

These can be illustrated in Figure 1

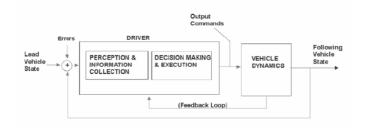


FIGURE 1: Diagram of Car-following Components

As a result, if one can profoundly gain an insight into the car-following behaviors, there should be a way to mitigate and/or reduce the severity or the number of road accidents, especially rear-end collisions.

The objectives of this research are:

- To review the literature on car-following models, and road safety,
- To collect and analyze traffic data such as speeds and flows on the National Highway 7 or Chon Buri Motorway,
- To calibrate the GM 5<sup>th</sup> car-following model using a macroscopic approach,
- To analyze stability of the calibrated GM 5<sup>th</sup> car-following model,

• To provide the recommended following distance and a guideline for implementing the recommended following distance on national highways.

In the remainder of this paper, the proposed methodology to calibrate the GM 5<sup>th</sup> carfollowing model followed by the stability analysis of the car-following model based on the perturbation technique are presented. The calibration results, and their application to estimate the recommended following distance including a guideline for field implementation are discussed. The final conclusions and recommendations for future research are provided.

#### 2. LITERATURE REVIEW

There have long been many researchers investigating car-following models as they constitute the interaction among vehicles in the car-following mode. Car-following models are also one of the major ingredients of any traffic simulation models. It is found that most car-following models attempt to describe acceleration characteristics of the following wehicles in response to the change in motions of the leading vehicles. The GM car-following models are the most remarkable of all. There have been up to five versions of the GM models proposed since the 1950s. The parameter calibrations for these models are usually conducted using linear and nonlinear regression techniques. Maximum likelihood estimation to calibrate the models was proposed by Subramanian (1996) but the formulation of the GM 5<sup>th</sup> model was incorrectly specified. There are also other types of car-following models such as psychophysical and fuzzy-logic-based models but only a few of these have broadly been used in practice.

Reaction time for a car-following maneuver is the time lag between the detection of a stimulus and the application of the response. Further distinction is made in human factor research between reaction time and response time. The latter includes the duration of the response itself, while the former does not. Several studies have been conducted to estimate drivers' reaction times. Their results are summarized in the following table. The mean reaction times identifies in literature are rarely greater than 1.50 seconds.

Study	Mean Reaction Time (seconds)
Ranjikar et.al (2002)	1.23- 1.33
Gurusinghe et.al (2001)	1.50
Fambro et al (1998), Review	1.28
Fambro et al (1998)	1.10
Lerner et al (1995)	1.31
Ahmed (1999)	1.34

 TABLE 1: Summary of Reaction Time Estimation Results

Traffic stability conditions of the car-following models have been analyzed. There are two types of stability, namely 1) local stability, and 2) asymptotic stability. Asymptotic stability is more frequently discussed in literature as it provides information on interactions of each vehicle in the platoons. A Laplace Transforms technique is applied to determine stability conditions of traffic but limited to linear car-following models. In conclusions, the GM 5<sup>th</sup> model with an appropriate calibration method can be a good representative of the interaction of traffic in a car-following mode.

## **3. METHODOLOGY**

This section presents a methodology to calibrate the GM  $5^{\text{th}}$  car-following model based on the maximum likelihood estimation concept (MLE). As there always exists the relationship between car-following models and traffic stream models, first the macroscopic traffic stream model corresponding to the GM  $5^{\text{th}}$  car-following model is derived. Then, an error term is introduced into the relevant traffic stream model and assumed to be normally distributed so that macroscopic traffic data can be used to calibrate model parameters. Second, using the so-called perturbation technique the calibrated model is investigated to obtain a traffic stability condition.

#### 3.1 Maximum Likelihood Estimation of the Car-following Model

The speed-density relationship derived from the GM 5<sup>th</sup> car-following model is rewritten as follows.

$$v_i = v_f \cdot \left[ 1 - \left(\frac{k_i}{k_j}\right)^{\gamma - 1} \right]^{\frac{1}{1 - \beta}} + \varepsilon_i$$
(1)

where,

 $v_i$  is the average speed of traffic stream at the i th observed interval

 $k_i$  is the average density of traffic stream at the i th observed interval

- $\varepsilon_i$  is the error term corresponding to the i<sup>th</sup> observed interval
- $v_{\rm f}$  is the free flow speed
- k<sub>i</sub> is the jammed density

The error term is assumed to be i.i.d. normally distributed.

$$\varepsilon_{i} \sim N[0,\sigma^{2}]$$

$$f(\varepsilon_{i}) = \frac{1}{\sqrt{2\pi\sigma^{2}}} \cdot e^{-\frac{1}{2\sigma^{2}}\varepsilon_{i}^{2}}$$

$$\cos(\varepsilon_{i},\varepsilon_{j}) = \begin{cases} \sigma^{2} & \text{if } i = j \\ 0 & \text{otherwise} \end{cases}$$
(3)

Therefore, the likelihood function of N observation intervals is given by the product of Equation (2).

$$\begin{split} L(\beta,\gamma,v_{f},k_{j},\sigma^{2}) &= \prod_{i=1}^{N} f(\varepsilon_{i}) = \prod_{i=1}^{N} f(v_{i},k_{i}) \\ &= \prod_{i=1}^{N} \frac{1}{\sqrt{2\pi\sigma^{2}}} \cdot \exp(-\frac{1}{2\sigma^{2}} \cdot \left[ v_{i} - v_{f} \left[ 1 - \left(\frac{k_{i}}{k_{j}}\right)^{\gamma-1} \right]^{\frac{1}{1-\beta}} \right]^{2} \right) \\ &= \prod_{i=1}^{N} \frac{1}{(2\pi\sigma^{2})^{\frac{N}{2}}} \cdot \exp(-\frac{1}{2\sigma^{2}} \cdot \left[ v_{i} - v_{f} \left[ 1 - \left(\frac{k_{i}}{k_{j}}\right)^{\gamma-1} \right]^{\frac{1}{1-\beta}} \right]^{2} \right) \end{split}$$

The log-likelihood is then given by:

$$\ln L(\beta, \gamma, v_f, k_j, \sigma^2) = -\frac{N}{2} \ln(2\pi\sigma^2) - \frac{1}{2\sigma^2} \cdot \sum_{i=1}^{N} \left[ v_i - v_f \left[ 1 - \left(\frac{k_i}{k_j}\right)^{\gamma-1} \right]^{\frac{1}{1-\beta}} \right]^2$$
(4)

Maximizing ln L(-) results in the MLE estimates of the model parameters,  $\beta$ ,  $\gamma$ ,  $v_f$ ,  $k_j$ ,  $\sigma^2$ . In order to obtain standard errors of each parameter, information matrix, which is the negative of the expectation of the second order derivatives of the corresponding log-likelihood function, Equation (4), must be computed. This provides the lower bound for the standard errors of the parameters. After the calibration of the car-following parameters, the next step is to analyze the stability condition.

#### 3.2 Stability Analysis of the Car-following Model

Tailgating can produce particularly catastrophic results when a platoon of many consecutive tailgaters forms. This is because of intrinsic platoon dynamics which may amplify distances as they propagate down a line of vehicles. If the lead vehicle of a many vehicle platoon slow down gently and then regains its previous speed, the second vehicle may respond by slowing down more rapidly (depending on parameters such as reaction time and headway). The third vehicle will then be confronted with a more rapidly decelerating lead vehicle, so that as we progress down the platoon, each vehicle produces larger deceleration, until eventually braking capability is exceeded. For a sufficiently long platoon of vehicles with identical following parameters, a multiple-vehicle pile-up becomes inevitable. An individual driver in a platoon following at a large headway may damp out the disturbance so that no collisions occur. In general, the consequence of insufficient distances within vehicle platoons may be rear-end collisions, which are one of the most prevalent types of accidents in Thailand. Insufficient distances result from the inadequacy, partly due to human errors, of the drivers to maintain a distance which is adjusted to the speed. Hence, the safety of traffic flow could be enhanced if

the drivers were provided with information about the safe following distance. In this section, the formulation to estimate the following distance that guarantee asymptotic stability of traffic is derived.

For the ease of analysis, the governing equation of the car-following model (1) can be rewritten as follows

$$\mathcal{A}_{n+1}^{(k)}(t+T) = \frac{\alpha \mathcal{A}_{n+1}^{(k)}(t+T)}{(X_n(t) - X_{n+1}(t))^{\gamma}} (\mathcal{A}_n^{(k)}(t) - \mathcal{A}_{n+1}^{(k)}(t))$$
(5)

To examine the stability we perturb the equilibrium solution with a small deviation term  $\varepsilon$  as shown below.

$$X_{n}(t) = b \cdot n + v \cdot t + \varepsilon(n, t)$$
(6)

Where,

 $X_n(t)$  is the traveled distance of the n th vehicle at time t

b is the average distance between two consecutive vehicles at steady state

v is the speed of traffic stream at steady state

 $\varepsilon$  is the deviation from the steay state condition

In order to analyze the relative magnitude of the deviation between two consecutive vehicles in the car-following mode, we assume that  $\varepsilon(n,t) = f_n \cdot e^{i\omega t}$ . Substitute Equation (6) into Equation (5), we obtain the following.

$$\mathscr{K}(n+1,t+T) = \frac{\alpha \cdot [\nu + \mathscr{K}(n+1,t+T)]^{\beta}}{[b+\varepsilon(n,t)-\varepsilon(n+1,t)]^{\gamma}} \{\mathscr{K}(n,t) - \mathscr{K}(n+1,t)\}$$

 $\mathscr{K}(n+1,t+T) = \frac{\alpha \cdot [v]^{\beta}}{[b]^{\gamma}} \{\mathscr{K}(n,t) - \mathscr{K}(n+1,t)\} \text{ since } \varepsilon \text{ is very small when compared to } b \text{ and } v.$ 

 $\mathscr{K}(n+1,t+T) = \lambda \{\mathscr{K}(n,t) - \mathscr{K}(n+1,t)\} \quad \text{Let us define } \lambda \text{ as } \frac{\alpha \cdot [v]^{\beta}}{[b]^{\gamma}}$ 

$$e^{i\omega T}(i\omega)^2 f_{n+1} \cdot e^{i\omega t} = \lambda[(i\omega)e^{i\omega t}(f_n - f_{n+1})]$$
 since  $\varepsilon(n,t) = f_n e^{it\omega}$ .

$$\frac{J_{n+1}}{f_n} = \frac{\lambda}{i\omega \cdot e^{i\omega T} + \lambda}$$

Using the Euler's formula, we obtain

$$\frac{f_{n+1}}{f_n} = \frac{\lambda}{i\omega \cdot (\cos \omega T + i \cdot \sin \omega T) + \lambda}$$
$$\frac{f_{n+1}}{f_n} = \frac{\lambda}{i\omega \cos \omega T - \omega \sin \omega T + \lambda}$$
$$\left|\frac{f_{n+1}}{f_n}\right| \le 1; \qquad \frac{\lambda^2}{(\lambda - \omega \sin \omega T)^2 + (\omega \cos \omega T)^2} \le 1$$
$$2\lambda \omega \sin \omega T \le \omega^2 \sin^2 \omega T + \omega^2 \cos^2 \omega T$$
$$2\lambda \omega \sin \omega T \le \omega^2$$
$$\sin \omega T \le \frac{\omega}{2\lambda}$$

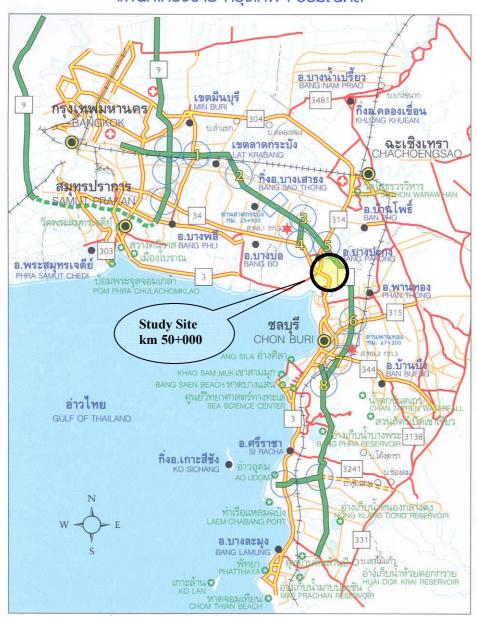
Taking the limit of  $\omega$  approaching zero, then we observe that stability occurs when

$$\lambda \cdot T \leq \frac{1}{2}$$
or 
$$\frac{\alpha \cdot [v]^{\beta}}{b^{\gamma}} \cdot T \leq \frac{1}{2}$$
(7)

Based on the perturbation technique, the stability condition of the GM 5<sup>th</sup> car-following model is derived. Equation (7) is the stability condition, which applies to all vehicles in a platoon at any given point in time and guarantees asymptotic stability of traffic flows.

#### 4. CALIBRATION RESULT AND ITS APPLICATION

The National Highway 7 was selected as the study facility because of its high volume and prevailing speed. The National Highway 7 or Chon Buri Motorway as it is commonly referred to, is a primary freeway facility located east of the Bangkok, and serves as a major corridor for local, regional, and national travels. Directional travel lanes along the Chon Buri Motorway are divided by grass medians. The posted speed limits on the Chon Buri Motorway are 120 km/h for passenger cars and 100 km/h for trucks, and 80 km/h for tractor-semitrailer combination trucks. Traffic volumes on the Chon Buri Motorway system are generally heavy during weekend morning and afternoon peak periods, and breakdowns in traffic flow are typical during these peak times. It is not uncommon for congested conditions to persist for several hours.



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FIGURE 2 : Map of the Study Facility

The Study Site is located in the vicinity of the Rest Area or Bang Pa Kong Interchange at km 50+000 toward Chon Buri. At this site, there are two eastbound travel lanes. Two detectors were installed approximately 200-meters downstream of the acceleration lane.



FIGURE 3: Snapshot of the Study Site

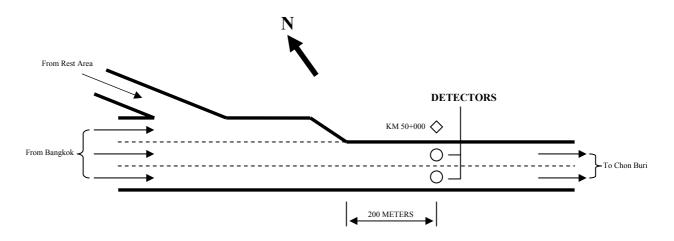
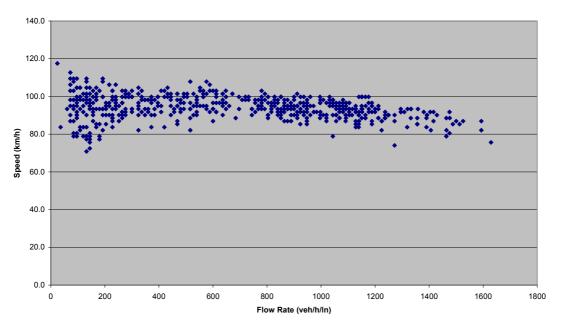
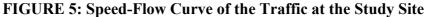


FIGURE 4: Schematic of the Study Site

Each detector station can continuously provide information on speeds, flows, densities, and proportions of heavy vehicles of the oncoming traffic in 5-minute intervals. Complete data sets were available for two days (March 23-24 and April 12-13, 2006). Free-flow speeds during off-peak periods were found to be 95 km/h. The percentage of heavy vehicles in the traffic stream in the area of the study site is roughly 5 percent. The study site regularly operates under uncongested conditions. Variations of the traffic demands and speeds throughout the study period resulted in different flows every day of the study. In addition, the speed-flow curve for this study site is developed and used as the basis for the GM carfollowing model calibration. Apparently, free-flow speed of the study site is approximately 95 km/h with the maximum observed flow of 1700 veh/h/ln. However, congested traffic conditions were not observed during the course of data collection.



Speed-Flow Curve of the Traffic on the National Highway 7 toward Chon Buri



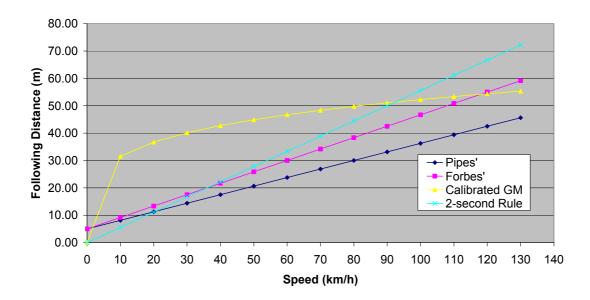
According to the maximum likelihood estimation technique, the parameter values are obtained through maximizing the log-likelihood function. Estimation results are provided in Table 2. The standard errors of each parameter are estimated using the Cramer-Rao lower bound, which provides a lower bound for the variance of any unbiased estimators.

Parameter	Mean	Standard Error	t-ratio
$\sigma^2$	33.646	2.238	15.034
v <sub>f</sub>	95.716	0.080	1,196.450
kj	116.067	1.482	78.318
γ	4.510	0.042	107.143
β	0.990	0.00002	49500.000

**TABLE 2: Car-following Parameter Estimation Based on MLE** 

Apparently from the results, each parameter is statistically different from zero at 95% level of confidence as all t-ratios are greater than 1.96. The free-flow speed is approximately 96 km/h with the jammed density of 116 veh/km/ln. This is corresponding to a minimum spacing of 8.6 meters. Nonetheless, more data are needed to verify the significance of the jammed density because in this study only traffic data from the uncongested-regime are available in the calibration process.

In this study, it is assumed that the drivers' reaction time is 1.50 seconds because it is a conservative value of the reaction times according to the literature. Comparison among the well-known following distance rules is presented in Figure 6.



Following Distances Based on Different Car-Following Models

	Safe Following Distance (m)				
Speed (km/h)	Pipes'*	Forbes' <sup>*</sup>	Calibrated GM	2-second Rule	
0	5.00	5.00	0.00	0.00	
10	8.13	9.17	31.52	5.56	
20	11.25	13.33	36.70	11.11	
30	14.38	17.50	40.12	16.67	
40	17.50	21.67	42.74	22.22	
50	20.63	25.83	44.88	27.78	
60	23.75	30.00	46.71	33.33	
70	26.88	34.17	48.32	38.89	
80	30.00	38.33	<i>49.76</i>	44.44	
90	33.13	42.50	51.06	50.00	
100	36.25	46.67	52.26	55.56	
110	39.38	50.83	53.36	61.11	
120	42.50	55.00	<i>54.39</i>	66.67	
130	45.63	59.17	55.35	72.22	

\* Assume average vehicle length of 5 meters.

Recommended following distances

#### FIGURE 6: Comparison of Recommended Following Distances

#### **Based on Different Models**

There are four models considered namely, 1) Pipes's model, 2) Forbes's model, 3) two-second rule, and 4) our calibrated GM model. When speeds are lower than 90 km/h, the recommended following distances of the calibrated GM model are greater than those of the other models. However, when speeds are greater than 90 km/h, except for the Pipes' and the Forbes's model, the recommended following distances of the calibrated GM model are lower than those of the two-second rule. It is worth noting that the calibrated GM model provides better estimates of the following distances since other models do not account for unstable behaviors of drivers. The calibrated model is also based on traffic information collected in

Thailand. The following distances are recommended for the speed range from 80 to 120 km/h at which the data are collected. This speed range is commonly observed on national highways.

In order to bring the findings of this research into practice, the "dot" tailgating treatment marking is deployed as a safety countermeasure for assisting drivers in establishing recommended following distances. This treatment should be promoted in sections of roads or corridors with higher than average numbers of crashes linked to aggressive driving or tailgating and where traffic congestion is not anticipated. Markings are spaced such that a minimum of two markings separate vehicles, which allows for a recommended distance between them. A guideline for implementing this "dot" tailgating treatment marking is created in a form of drawings. Please note that these drawings are not an ultimate recommendation for practice but it is merely meant to be a starting point for a better research and implementation (please see Figure 7 for details).

Following the same terminology used in FHWA (2003), there are some terms denoted in the guideline drawings

- 1. Comprehension Time (seconds): Amount of time required for driver to comprehend the meaning of the markings.
- 2. Perception and Reaction Time (seconds): Indicates time required for an average driver on target roadway to perceive that an action is required and to begin that action. Typical value is 2.5 seconds (from Green Book 2004). This P/R time is different from the reaction time in a usual car-following maneuver.
- 3. Adjustment Time (seconds): Amount of time provided for the following driver to gauge and adjust the distance between their vehicle and the lead vehicle.
- 4. Effective Time (seconds): Length of time for which the pattern maintains an effort on the driver. Relates to how long the driver can maintain the distance after leaving the pattern.
- 5. Posted Speed Limit (km/h): related to the posted speed limit on the target roadway.
- 6. Marking Spacing, S (meters): this distance reflects the spacing between two pavement markings within the pattern such that vehicle will traverse two markings in the following time. Value is equal to the recommended following distance from Figure 6 less the vehicle correction.
- 7. Vehicle Correction (meters): the distance vehicle must be away from the nearest dot to allow the dot to be visible from the drivers' eye position. This value assumed to be 4.5 meters measured from the bumper to the edge of the dot marking as shown in Figure 9.
- 8. Number of Markings in Pattern: the number of markings at the marking spacing that can be placed in the length of roadway required to travel at the posted speed for the total required comprehension, perception and reaction, and adjustment times. Value is that length (meters) divided by marking spacing (meters).
- 9. Pattern Length, L (meters): the distance from the center of the first marking in the pattern to the center of the last marking in the pattern. Value is the number of markings, less one, times marking spacing.
- 10. Pattern Spacing, X (meters): the distance a vehicle will travel between marking patterns. Relates to effective time such that the effect of the previous set of markings will just begin to fade as driver encounters the next set. Value is posted speed limit times effective time.

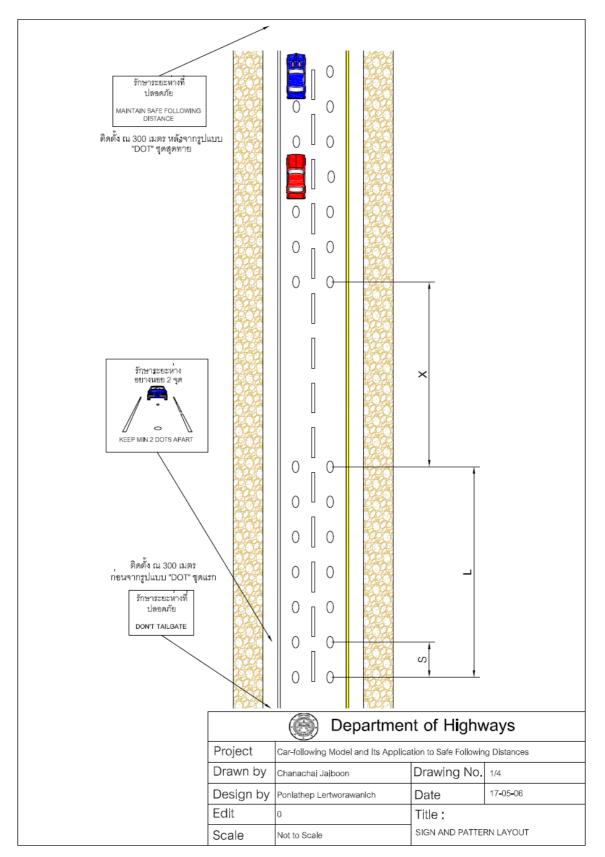
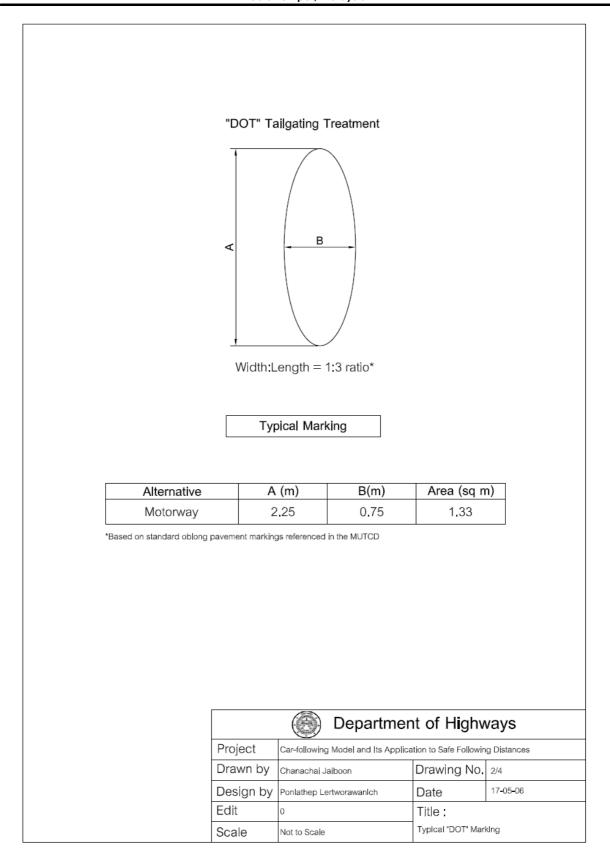
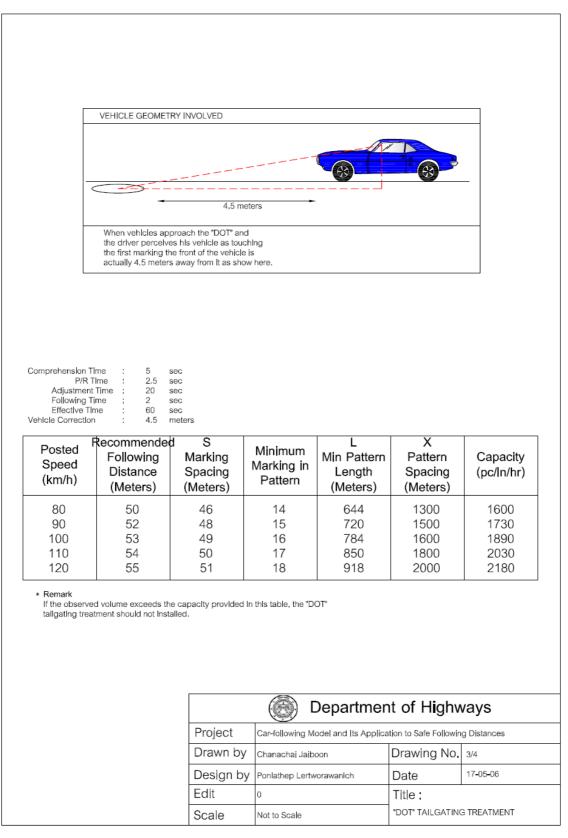


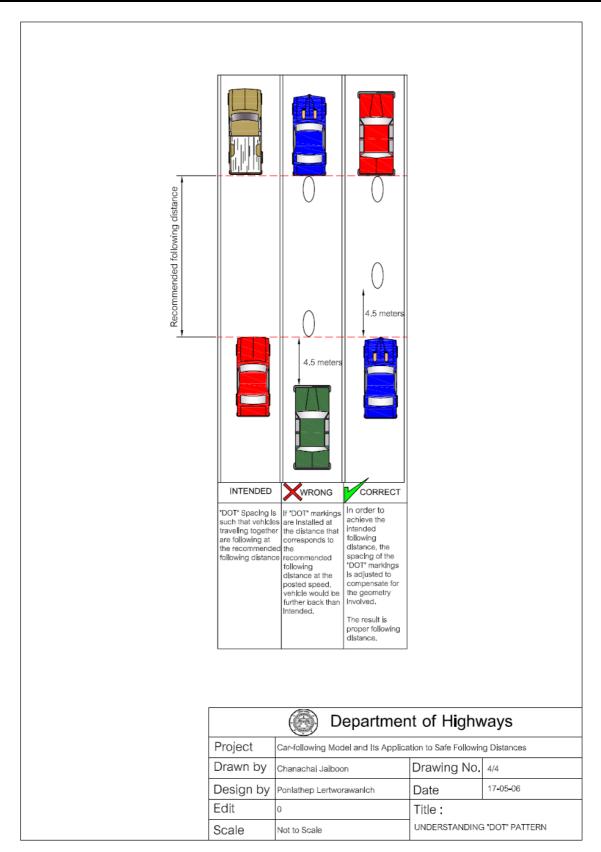
FIGURE 7: Sign and Pattern Layout



## FIGURE 8: Typical "DOT" Marking



## FIGURE 9: "DOT" Tailgating Treatment



## FIGURE 10: Understanding "DOT" Pattern

#### 5. CONCLUSIONS AND FUTURE RESEARCH

A rear-end collision, often called simply rear-end, is a traffic accident where a vehicle impacts the vehicle in front of it. Typical scenarios for rear-ends are: i) a sudden deceleration by the first car, for example, to avoid someone crossing the street, ii) the following car that does not have the adequate time to brake and impacts the first and iii) at a road junction the following car accelerates more rapidly than the leading. Upon the completion of this research, the following conclusions were drawn:

- The GM 5<sup>th</sup> car-following model was calibrated based on a macroscopic traffic stream model using traffic data collected at the Nation Highway 7.
- MLE technique can be used to calibrate the GM  $5^{th}$  car-following model.
- The perturbation technique can be used to derive the asymptotic stability condition of the GM 5<sup>th</sup> car-following model.
- The recommended following distance was developed from a speed range from 80 km/h to 120 km/h with guideline drawings for field implementation.

In addition, the following research needs to enhance the analyses of the car-following models for estimating safe following distances are identified as follows:

- Conduct an extensive data collection effort that can provide information on speeds and flows from both expressways and arterials so that both congested and uncongested traffic data are available.
- Conduct data collection using an aerial photograph technique so that microscopic information such as location, speed and acceleration of each vehicle at the study site can be evaluated.
- Develop a methodology based on panel data analysis in such a way that drivers' reaction times can be calibrated.
- Experiment with the "dot" tailgating treatment marking to evaluate its effectiveness in practice.
- Integrate the findings of this research into future editions of the DOH standard drawings after the experiment indicates the effectiveness of the "dot" tailgating treatment marking.

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